

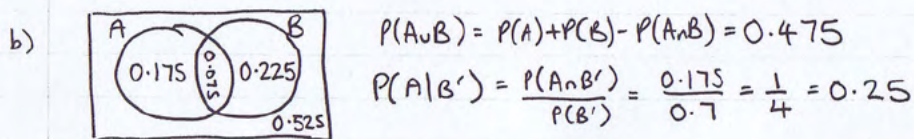
1a) Cheaper / Easier to collect results from a sample. These results can be statistically analysed and providing the sample was unbiased be extended to the whole population.

b) i) Normal distribution ii) Discrete Uniform Distribution.

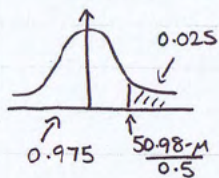
2 $P(AAA) = \frac{60}{125} \times \frac{59}{124} \times \frac{58}{123} = 0.108$ (10.8%)

b) $P(AAS) + P(ASA) + P(SAA) = 3 \times P(AAS) = 3 \times \frac{85}{125} \times \frac{84}{124} \times \frac{40}{123} = 0.449$ (45%)

3 If Independent $P(A \cap B) = P(A) \times P(B) = 0.25 \times 0.3 = 0.075$



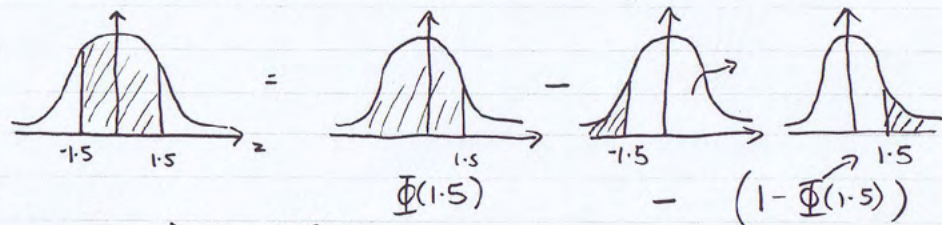
4 $L \sim N(\mu, 0.5^2)$ $Z = \frac{L - \mu}{\sigma}$



$P(L > 50.98) \Rightarrow P(Z > \frac{50.98 - \mu}{0.5}) = 0.025$
 $\Rightarrow P(Z < \frac{50.98 - \mu}{0.5}) = 0.975 = \Phi(1.96)$

$\Rightarrow \frac{50.98 - \mu}{0.5} = 1.96 \Rightarrow \mu = 50.98 - \frac{1.96}{2} = 50$ ✓

b) $P(49.25 < L < 50.75) \Rightarrow P(\frac{49.25 - 50}{0.5} < Z < \frac{50.75 - 50}{0.5})$
 $\Rightarrow P(-1.5 < Z < 1.5)$



$= 2\Phi(1.5) - 1 = 0.8664$

So $P(L > 50.75)$ or $P(L < 49.25) = 1 - 0.8664 = 0.1336$

$P(2 \text{ Unusable}) = 0.1336 \times 0.1336 = 0.0178$ (1.8%)

5) $n=8, \bar{s} = \frac{\sum s}{n} = 6.06 \quad \bar{t} = \frac{\sum t}{n} = 8.125$

$S_{ss} = \sum s^2 - \frac{(\sum s)^2}{n} = 108.08$ and $S_{tt} = 173.68, S_{st} = 10$

$y = a + bx, b = \frac{S_{st}}{S_{xx}} \quad a = \bar{y} - b\bar{x}$ so $t = p + qs \Rightarrow q = \frac{S_{st}}{S_{ss}} = 1.195$

$t = 0.88 + 1.195s$

$p = \bar{t} - q\bar{s} \Rightarrow p = 0.88$

b) $s = x - 6 \Rightarrow y - 20 = 0.88 + 1.195(x - 6) \Rightarrow y = 20.88 + 1.195x - 7.17$
 $y - 20 = t \Rightarrow y = 13.71 + 1.195x$

c) PMCC for x and y is the same as s and t since to go from $(x, y) \rightarrow (s, t)$ each point is moved 6 left and 20 down, i.e. gradient of the least squares regression line will be identical.

$r = \frac{S_{st}}{\sqrt{S_{ss}S_{tt}}} = 0.943$

6 $x \quad -2 \quad -1 \quad 0 \quad 1 \quad 2$ a) $E(x) = -2\alpha - 0.2 + 0.2 + 2\beta = -0.2$
 $P(X=x) \propto \alpha \quad 0.2 \quad 0.1 \quad 0.2 \quad \beta \Rightarrow \alpha - \beta = 0.1 \Rightarrow \alpha = 0.3$

$\sum P(X=x) = 1 \Rightarrow \alpha + 0.2 + 0.1 + 0.2 + \beta = 1 \Rightarrow \alpha + \beta = 0.5 \Rightarrow \beta = 0.2$

b) $F(0.8) = P(-2) + P(-1) + P(0) = \alpha + 0.2 + 0.1 = 0.6$

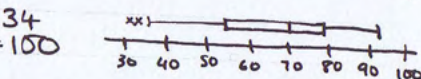
c) $\text{Var}(x) = E(x^2) - [E(x)]^2 \Rightarrow 2.4 - (-0.2)^2 = 2.36$
 $E(x^2) = 4 \times 0.3 + 1 \times 0.2 + 1 \times 0.2 + 2 \times 0.2 = 2.4$

d) $E(3x - 2) = 3E(x) - 2 = -2.6 \quad \text{Var}(2x + 6) = 2^2 \text{Var}(x) = 9.44$

7) Mode = 78, $n=50 \Rightarrow Q_1 = x_{13} = 56 \quad Q_2 = \frac{1}{2}(x_{25} + x_{26}) = 70 \quad Q_3 = x_{38} = 77$

$IQR = Q_3 - Q_1 = 22 \quad Q_1 - 1.0(Q_3 - Q_1) = 34$
 $Q_3 + 1.0(Q_3 - Q_1) = 100$

$\mu^2 = \frac{\sum x^2}{n} - \mu^2 = 242.19 \Rightarrow \sigma = 15.56$



Skew = $3\frac{(\mu - Q_2)}{\sigma} = -0.53$

Weakly negative skew

Negative skew if $Q_2 - Q_1 > Q_3 - Q_2$

$Q_2 - Q_1 = 14 \quad Q_3 - Q_2 = 8 \quad 14 > 8$ so negative skew